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## Operational Amplifier Op-Amp

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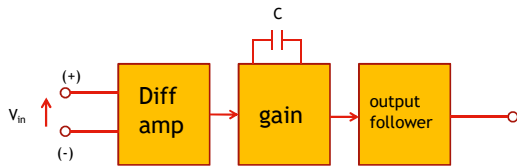
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## Op-Amp block diagram



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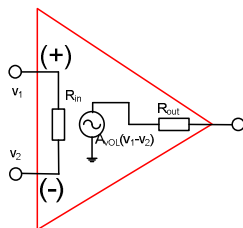
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## Op-Amp model



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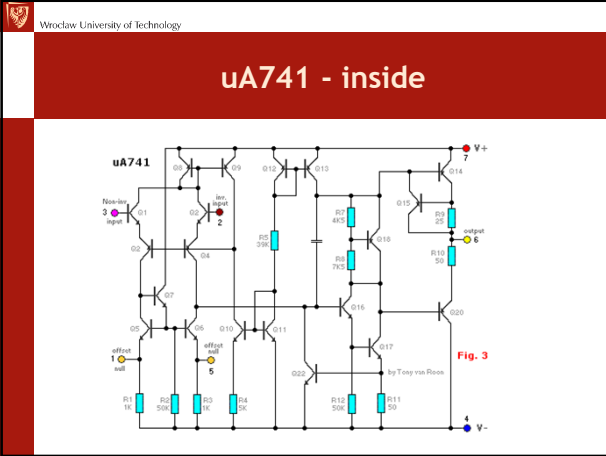
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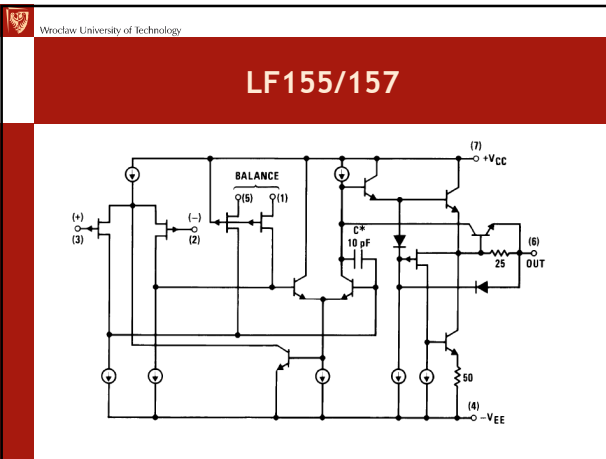
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## Typical Op-Amp parameters

Parameter	Symbol	Perfect op-amp	uA741	LF157
OL gain	$A_{VOL}$	infinite	100000	200000
Unity gain frequency	$f_T$	infinite	1Mhz	20MHz
Input resistance	$R_{in}$	infinite	2M $\Omega$	10 <sup>12</sup> $\Omega$
Output resistance	$R_{out}$	zero	75 $\Omega$	100 $\Omega$
Input bias	$I_{in(bias)}$	zero	80nA	30pA
Input offset current	$I_{in(off)}$	zero	20nA	3pA
Input offset voltage	$V_{in(off)}$	zero	2mV	1mV
CMRR	CMRR	infinite	90dB	100dB

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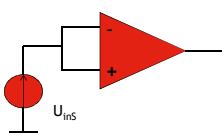
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## Common Mode Rejection Ratio

$$V_{out} = A_v V_{DIFF} + \frac{A_v}{CMRR} V_{CM}$$


$$V_{OUT} = \frac{A_v}{CMRR[V/V]} V_{inS}$$

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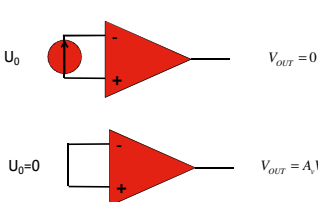
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## Input offset voltage




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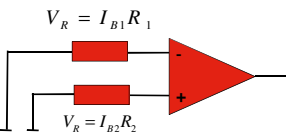
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## Voltage offset vs. input bias current



$$V_{out(off)} = (I_B (R + \Delta R) - (I_B + \Delta I_B) R) A_v =$$

$$= (\Delta I_B R + I_B \Delta R) A_v \underset{\Delta R=0}{\approx} \Delta I_B R A_v$$


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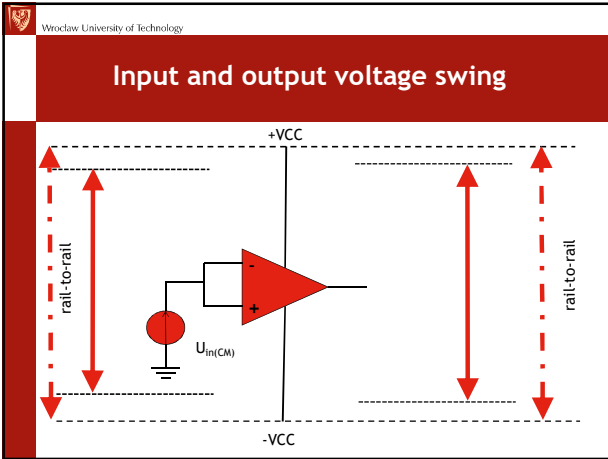
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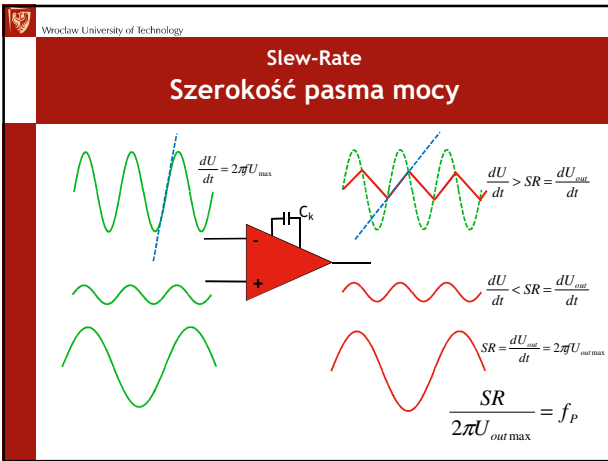
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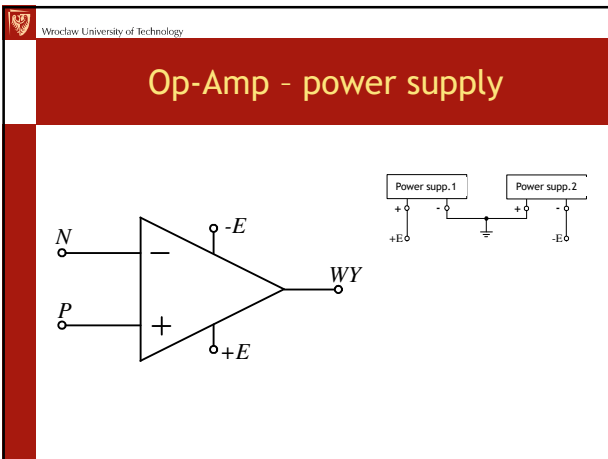
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## Op-Amp common applications

- inverting amp,
- Non-inverting amp
- summing amp
- substracting amp
- integrator
- differentiator

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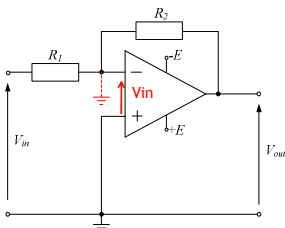
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## Inverting Amp virtual ground



For a perfect OA:

$$A_{v,OL} = \infty$$

$$r_{in} = \infty$$

so:

$$V_{in} = \frac{V_{out}}{A_{v,OL}} = \frac{V_{out}}{\infty} = 0$$

$$I_{in} = \frac{V_{in}}{r_{in}} = \frac{V_{in}}{\infty} = 0$$

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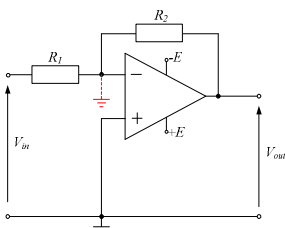
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## Inverting Amp



$$I_{in} = \frac{V_{in}}{R_1} \quad I_{out} = \frac{V_{out}}{R_2}$$

$$I_{in} = -I_{out}$$

$$\frac{V_{in}}{R_1} = -\frac{V_{out}}{R_2}$$

$$A_v = \frac{V_{out}}{V_{in}} = -\frac{R_2}{R_1}$$

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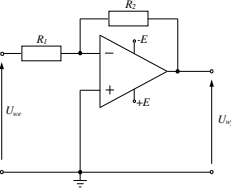
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## inverting amp (in detail)



$$A_v = -\frac{R_2}{R_1} \frac{1}{1 + \frac{R_1 + R_2}{A_{v,OL} R_1}} \approx -\frac{R_2}{R_1}$$

$$R_{in} = R_1 \frac{1}{1 + \frac{|A_v|}{A_{v,OL}}} \approx R_1$$

$$R_{out} = R_{out0} \frac{R_1 + R_2}{R_1(1 + A_{v,OL}) + R_2} \approx R_{out0} \left| \frac{A_v}{A_{v,OL}} \right|$$

$$f_2 \approx \frac{f_T}{A_v}$$

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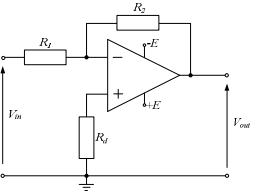
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## Bias current compescation



$$R_d = \frac{R_1 R_2}{R_1 + R_2}$$

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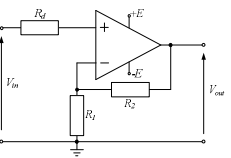
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## non-inverting amp



$$A_v = \left(1 + \frac{R_2}{R_1}\right) \frac{1}{1 + \frac{R_1 + R_2}{A_{v,OL} R_1}} \approx 1 + \frac{R_2}{R_1}$$

$$R_{in} = R_{in0}$$

$$R_{out} = \frac{R_{out0}}{A_{v,OL}}$$

$$f_2 \approx \frac{f_T}{A_v}$$

$$R_d = \frac{R_1 R_2}{R_1 + R_2}$$

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## Follower

$$A_v = \left(1 + \frac{R_2}{R_1}\right) \frac{1}{1 + \frac{R_1 + R_2}{A_{v,OL} R_1}} \approx 1 + \frac{R_2}{R_1}$$

$$f_2 = f_T$$


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## Frequency characteristic

$$f_2 A_v = f_T \cdot "1"$$


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## Summing amp

$$V_{out} = -R_2 \sum_{k=1}^N \frac{V_{in_k}}{R_{1k}} = - \left( V_{in1} \frac{R_2}{R_{11}} + V_{in2} \frac{R_2}{R_{12}} + V_{in3} \frac{R_2}{R_{13}} + \dots + V_{inN} \frac{R_2}{R_{1N}} \right)$$


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## Sumator odwracający

$$V_{out} = -R_2 \sum_{k=1}^N \frac{V_{in_k}}{R_{1k}} = - \left( V_{in1} \frac{R_2}{R_{11}} + V_{in2} \frac{R_2}{R_{12}} + V_{in3} \frac{R_2}{R_{13}} + \dots + V_{inN} \frac{R_2}{R_{1N}} \right)$$

when:  $R_{11} = R_{12} = R_{13} = \dots = R_{1N} = R_1$

$$V_{out} = - \frac{R_2}{R_1} (V_{in1} + V_{in2} + V_{in3} + \dots + V_{inN})$$

$$R_d = R_2 \parallel R_{11} \parallel R_{12} \parallel R_{13} \parallel \dots \parallel R_{1N}$$


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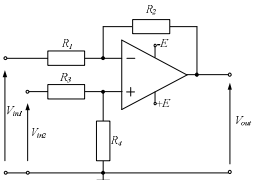
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## Subtractor (DIFFERENCE AMPLIFIER)



$$V_{out} = V_{in2} \left( \frac{R_1 + R_2}{R_3 + R_4} \right) \frac{R_4}{R_1} - V_{in1} \frac{R_2}{R_1}$$

when:  $R_1 = R_3$  and  $R_2 = R_4$

$$V_{out} = \frac{R_2}{R_1} (V_{in2} - V_{in1})$$

$$R_{in1} \approx R_1$$

$$R_{in2} = R_3 + R_4$$


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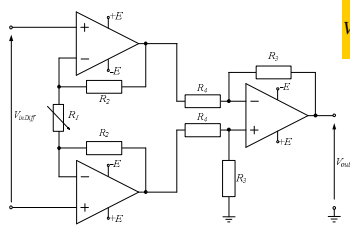
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## Instrumentation Amp



$$V_{out} = \left( 1 + 2 \frac{R_2}{R_1} \right) \frac{R_4}{R_3} V_{inDiff}$$


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## Instrumentation Amp

offset voltage can be applied

$$V_{out} = (V_{in2} - V_{in1}) \left( 1 + \frac{R_1}{R_2} + \frac{2R_1}{R_G} \right)$$


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## Integrator

$$I_{we} = \frac{U_{we}(t)}{R} \quad I_{in} = I_c = C \frac{dV_{out}(t)}{dt}$$

$$I_{in} = -I_{out}$$

$$V_{out}(t) = -\frac{1}{RC} \int V_{in}(t) dt + U_0$$

$$V_{out} = -\frac{V_{in}}{R_1 C} t + U_0$$


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## Differentiator

$$I_{in} = C \frac{dV_{in}(t)}{dt} \quad I_{out} = \frac{V_{in}(t)}{R}$$

$$I_{in} = -I_{out}$$

$$V_{out}(t) = -RC \frac{dV_{in}(t)}{dt}$$


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### phase shifter (all pass filter of 1st order)

$$\frac{V_{out}}{V_{in}} = -\frac{1 - sCR_2}{1 + sCR_2}$$


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### current - voltage transducer

$$V_{out} = -I_{in}R$$


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### Voltage - current transducer

$$I_L = \frac{V_{cc} - V_{in}}{R}$$


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## Voltage - current transducer (2)

$$I_L = \frac{V_{in}}{R_1} + \frac{R_2 - R_3}{R_1 R_3} V_{out} = \frac{V_{in}}{R_1 R_3 R_3}$$


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## INIC (Current Negative Impedance Converter)

$$I_{in} = \frac{V_{out} - V_{in}}{R_3} = \frac{V_{in} \left( \frac{R_2}{R_1} + 1 \right) - V_{in}}{R_3} = \frac{R_2}{R_3 R_1} V_{in}$$

$$R_{in} = -R_3 \frac{R_2}{R_1}$$


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## Gyrator

Gyrator Simulating a 1 H Inductor

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## Girator

$L = R_1 R_2 C$   
 $F = \frac{1}{2\pi R_1 R_2 C} = 1524 \text{ Hz}$

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## Auto-zero Amp ???

**TIPS:**  
 • low operatin frequency,  
 • very low offset

NOTE: Internal capacitors. No external capacitors required.

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## Summing up

- real and perfect Op-Amp parameters,
- applications:
  - inverting and non-inverting amp,
  - summing amp and subtracting amp,
  - instrumentation amp,
  - integrator and differentiator,
  - idea of an auto zero amp ??

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