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## Active filters



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## Active filters

Electronic filters are circuits with signal processing functions, they remove unwanted frequency to enhance wanted ones.

Electronic filters can be:

- passive or active (LC (SAW -Surface Acoustic Wave) OR with active elements e.g. Op-Amp)
- analogue or digital (Digital Signal Processing) or switched capacitor



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## Active filters realization

Active filters can be realized as:

- continuous time filters - analogue filters
- switched capacitor filters



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## Active filters

Frequency specification:

- high-pass,
- low-pass,
- band-pass,
- band-stop (band-rejection; notch),
- all-pass (usually specific phase transmission)



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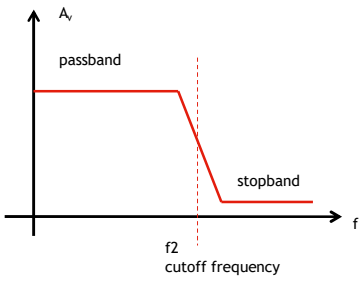
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## Low-Pass filter



The graph shows the gain  $A_v$  on the vertical axis and frequency  $f$  on the horizontal axis. A horizontal line represents the passband. At the cutoff frequency  $f_2$ , the gain begins to drop, forming a slope that leads to a lower horizontal line representing the stopband.



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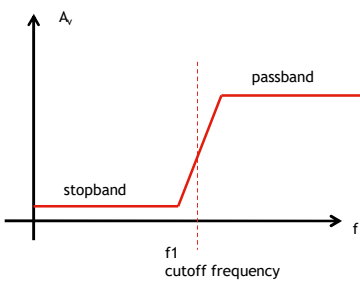
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## High-Pass filter



The graph shows the gain  $A_v$  on the vertical axis and frequency  $f$  on the horizontal axis. A horizontal line at a low level represents the stopband. At the cutoff frequency  $f_1$ , the gain begins to rise, forming a slope that leads to a higher horizontal line representing the passband.



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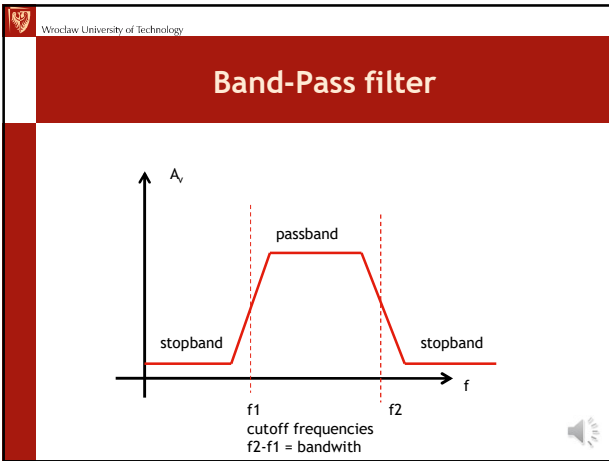
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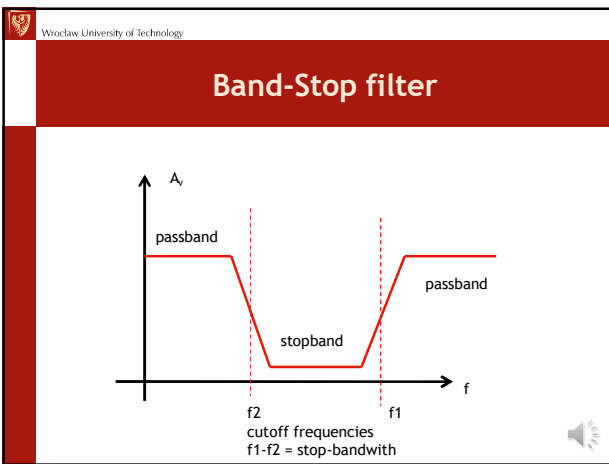
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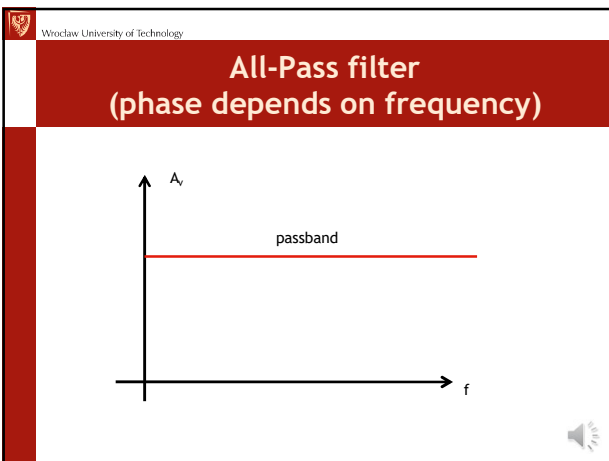
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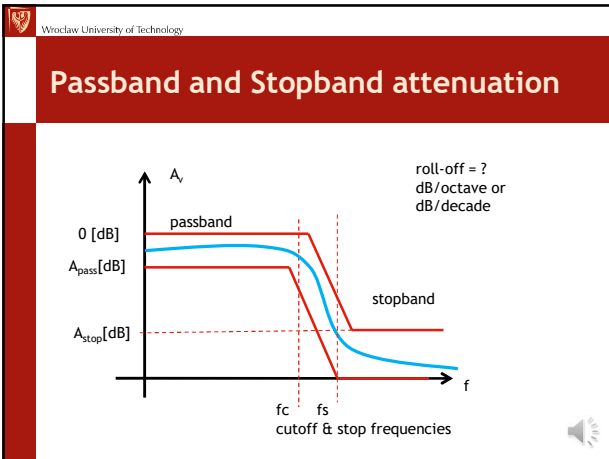
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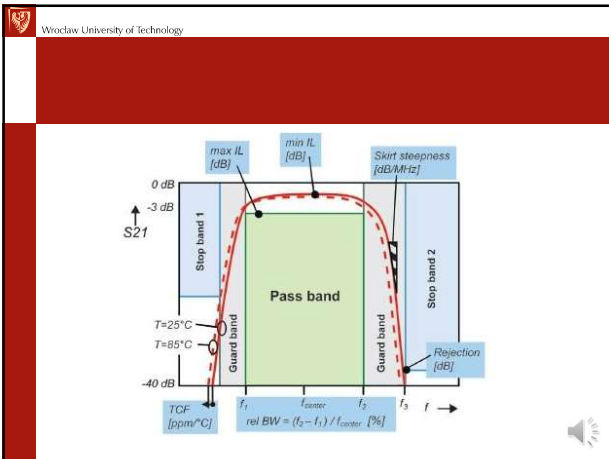
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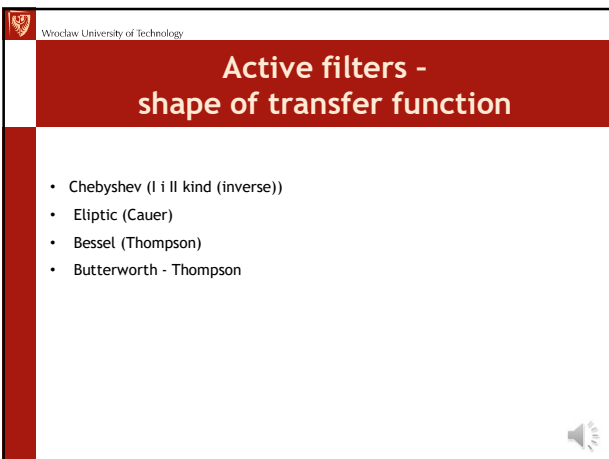
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## Order of a filter

$$H(s) = \frac{U_{out}(s)}{U_{in}(s)} = \frac{a_n s^m + a_{m-1} s^{m-1} + \dots + a_0}{b_n s^n + b_{n-1} s^{n-1} + \dots + b_0} = \frac{a_m \prod_i (s - z_i)}{b_n \prod_j (s - p_j)}$$

n = number of capacitors and inductances (LC - filter)  
 n = number of capacitors (RC - filters)




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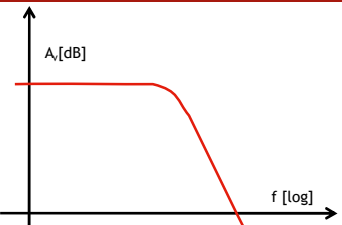
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## Butterworth approximation pass-band max flatness



max flatness of pass-band  
 Roll-off = 20\*n dB/decade  
 Roll-off = 6\*n dB/octave  
*-for low & high -pass*  
*-½ for stop & pass -band*  
 Phase/impulse response = acceptable




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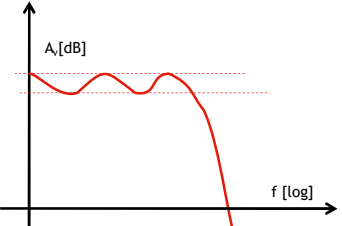
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## Chebyshev (I) approximation pass-band ripples



No. Ripples = n/2  
 Roll-off > 20n dB/decade  
 Roll-off > 6n dB/octave  
 Phase/impulse response = bad




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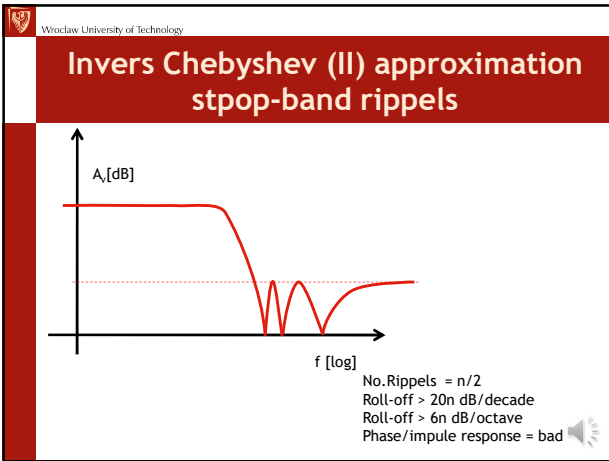
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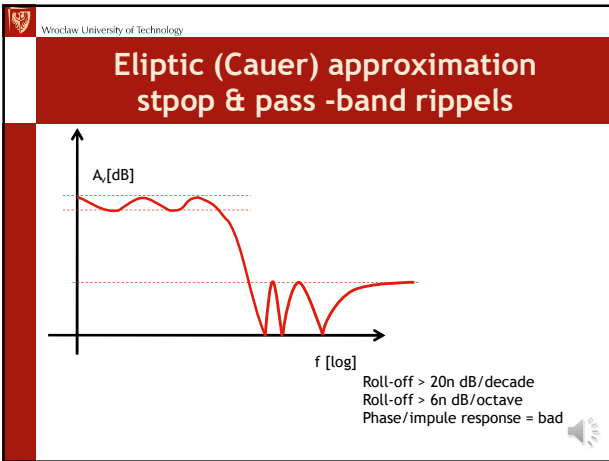
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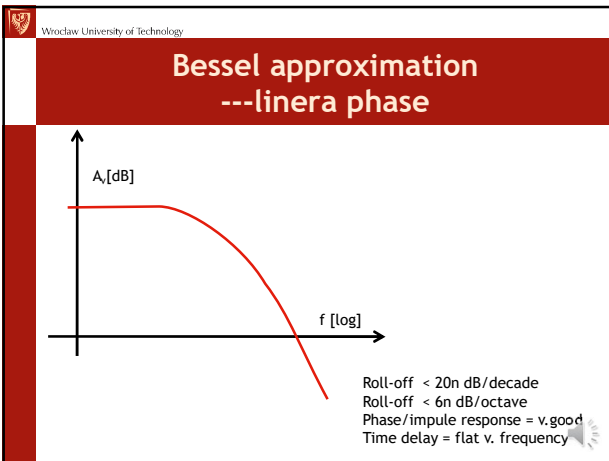
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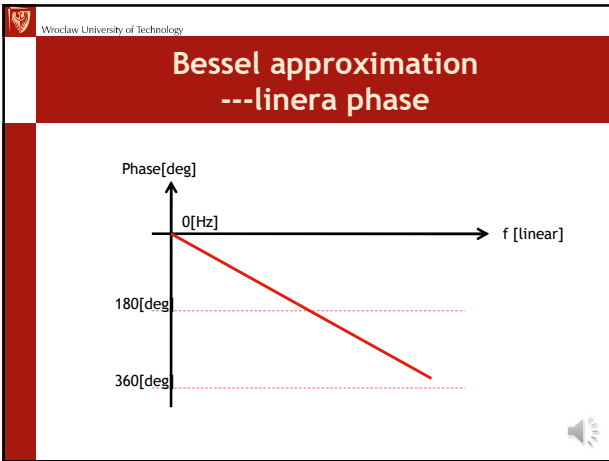
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### 6th order filter attenuation

← octave →

Type	f2 [dB]	2*f2 [dB]
Bessel	3	14
Butteworth	3	36
Chebyshev	3	63
Invers Chebyshev (II)	3	63
elliptic	3	93

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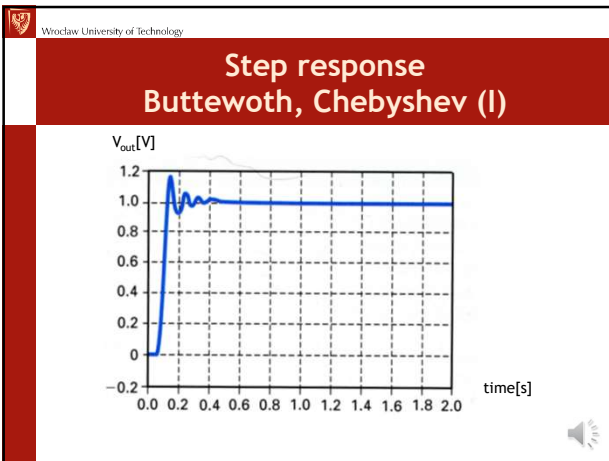
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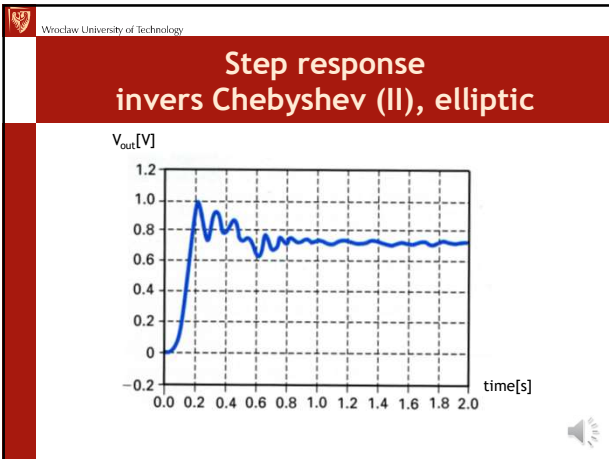
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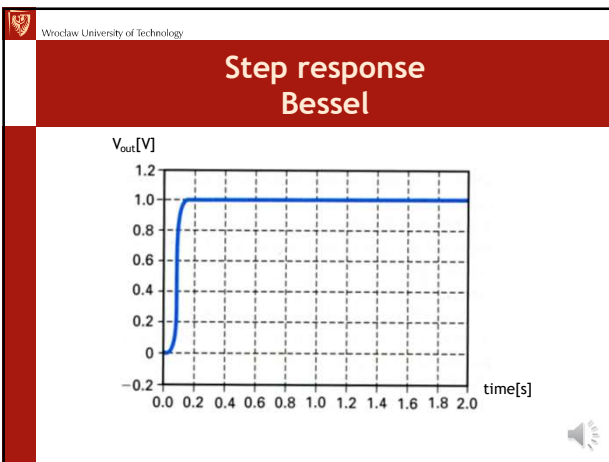
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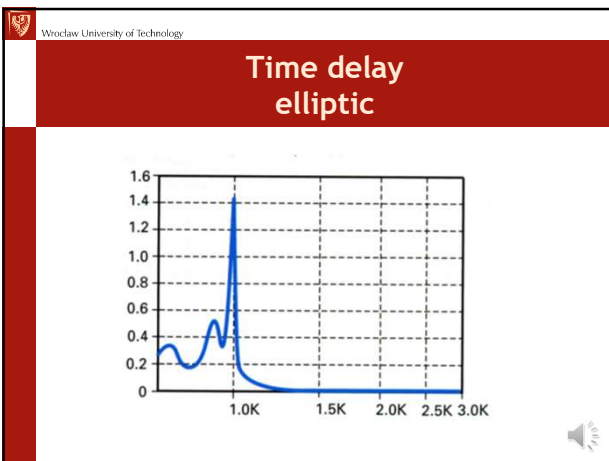
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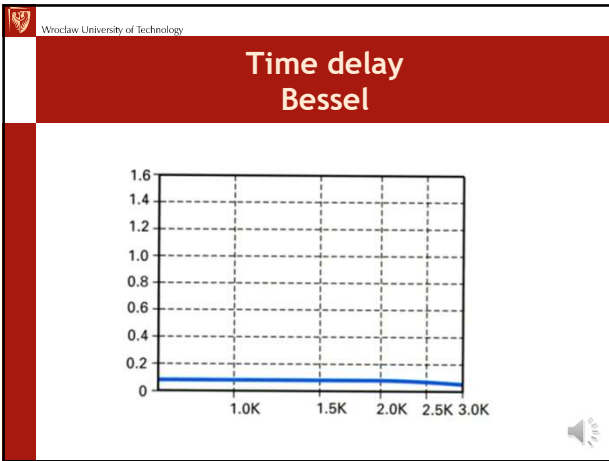
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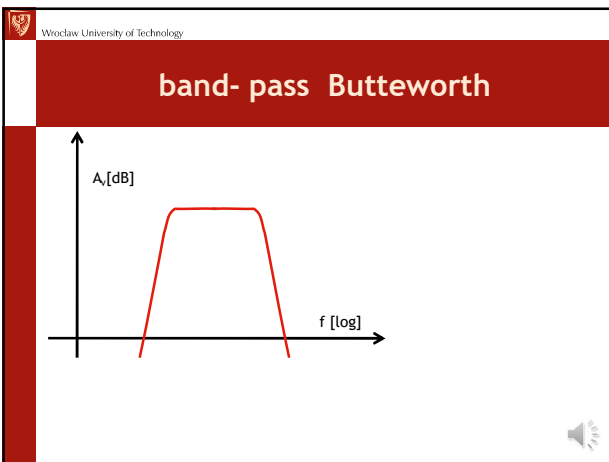
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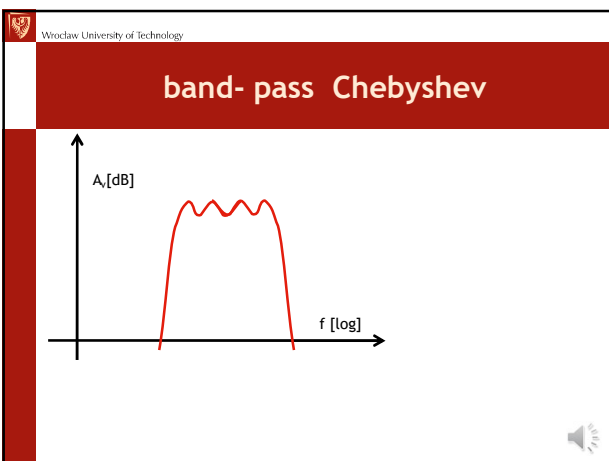
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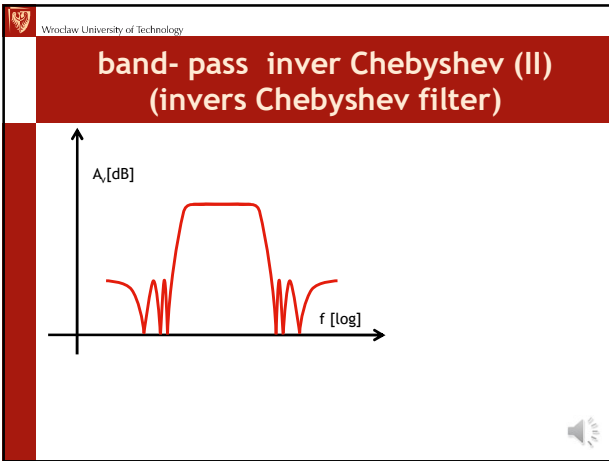
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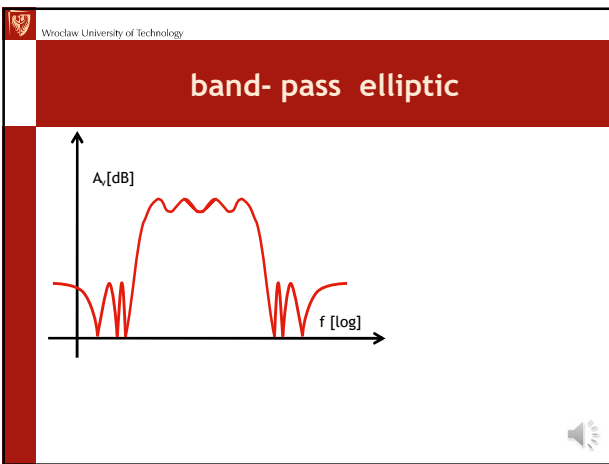
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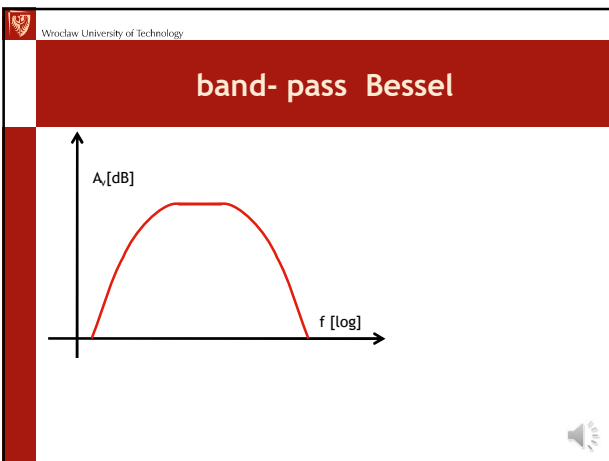
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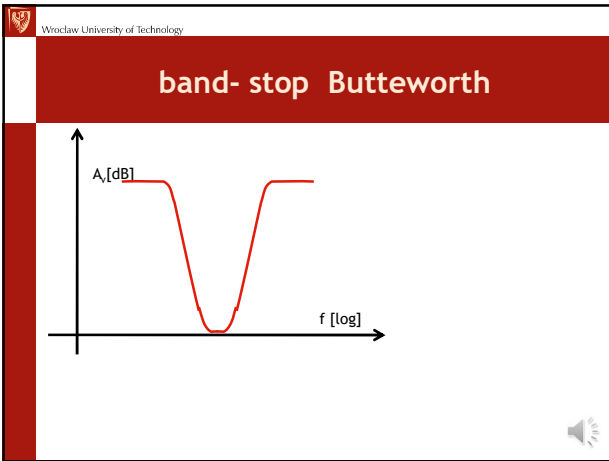
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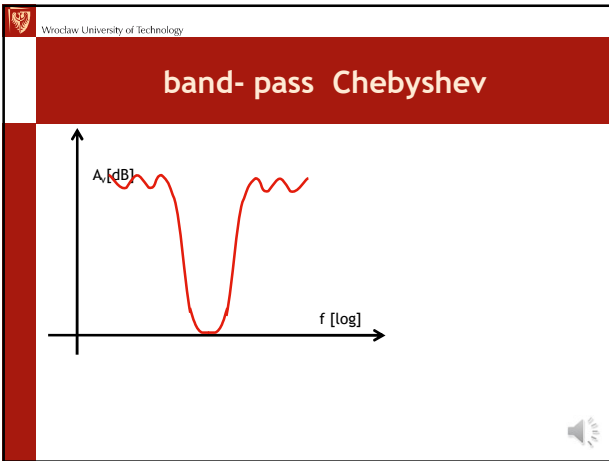
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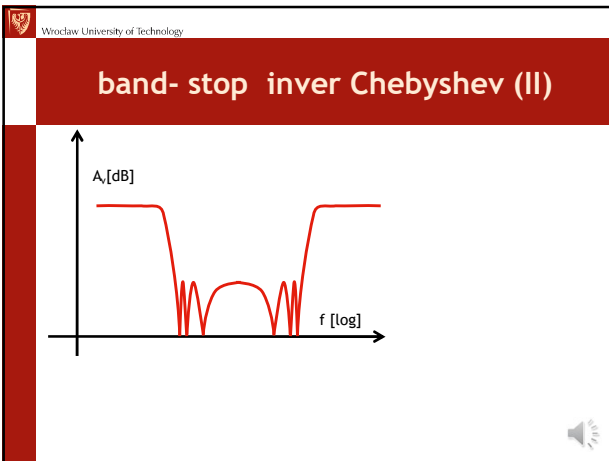
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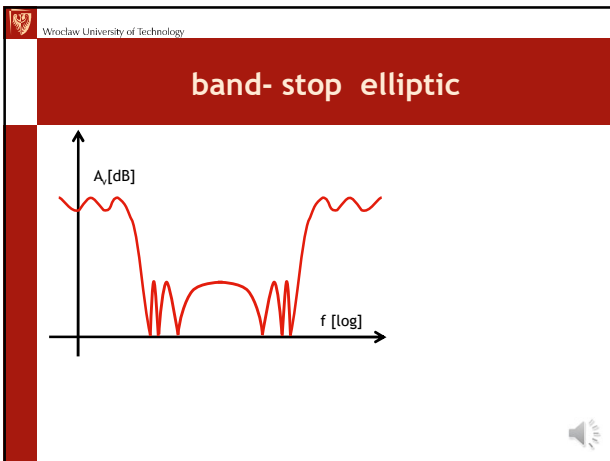
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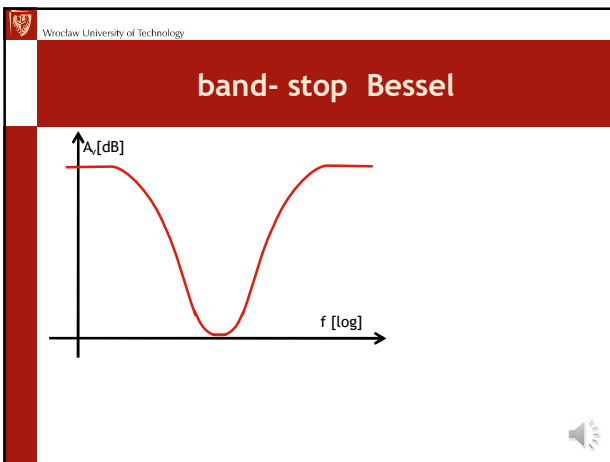
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### Filter approximation general features

Type	passband	stopband	Roll-off	Step response
Bessel	flat	monotonic	poor	best
Butterworth	flat	monotonic	good	good
Chebyshev	rippled	monotonic	v. good	poor
ln.Chebyshev (II)	flat	rippled	best	poor
Elliptic (Cauer)	rippled	rippled	best	v.poor

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## Active filter implementation




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## Active filters - introduction


Transmittance:

$$H(s) = \frac{U_{out}(s)}{U_{in}(s)} = \frac{a_m s^m + a_{m-1} s^{m-1} + \dots + a_0}{b_n s^n + b_{n-1} s^{n-1} + \dots + b_0} = \frac{a_m \prod_i (s - z_i)}{b_n \prod_j (s - p_j)}$$

$a_i, b_j$  - real numbers  
 $z_i, p_j$  - zeros and poles of transmittance

$$H(s) = |H(\omega)| \exp[j\varphi(\omega)]$$

$|H(s)|$  - amplitude transmittance  
 $\varphi(s)$  - phase transmittance




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## Active filters - introduction c.d.

Transmittance factorization:

$$H(s) = \frac{N(s)}{D(s)} = \prod_k H_k(s) = \prod_k \frac{N_k(s)}{M_k(s)}$$

Degree of  $N_k(s) \leq$  degree of  $M_k(s) \leq 2$

For  $M_k(s) = 2$  biquadratic section:

$$H_k(s) = \frac{a_2 s^2 + a_1 s + a_0}{s^2 + b_1 s + b_0} = \frac{N_k(s)}{s^2 + b_1 s + b_0}$$



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## Cascade of biquadratic filters

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## Active filters - intro

Biquadratic section can be expressed as:

$$H_k(s) = \frac{N_k(s)}{s^2 + \frac{\omega_0}{Q}s + \omega_0^2} = \frac{N_k(s)}{(s - p_1)(s - p_2)}$$

where:  $p_1, p_2$  - poles of the transmittance

For quality  $Q > 1/2$  poles are complex numbers

$$p_{1,2} = -\frac{\omega_0}{2Q} + j\frac{\omega_0}{2Q}\sqrt{4Q^2 - 1} = \sigma_p \pm j\omega_p$$

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## Active filters - intro

Real and imaginary parts are:

$$\sigma_p = -\frac{\omega_0}{2Q} \quad \omega_p = \omega_0 \sqrt{1 - \frac{1}{4Q^2}}$$

Specific frequency and quality are

$$\omega_0 = \sqrt{\sigma_p^2 + \omega_p^2} \quad Q = \frac{\sqrt{\sigma_p^2 + \omega_p^2}}{2|\sigma_p|} = \frac{\omega_0}{2|\sigma_p|}$$

Damping factor:

$$\alpha = \frac{1}{2Q}$$

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## Active filters - intro

When denominator is written in the form:


$$s^2 + b_1s + b_0 = s^2 + \frac{\omega_0}{Q}s + \omega_0^2$$

Parameters Q (quality) and  $\omega_0$  (characteristic frequency)

$$Q = \frac{\sqrt{b_0}}{b_1}$$

$$\omega_0 = \sqrt{b_0}$$

$b_0, b_1$  - real coefficients




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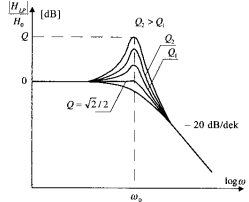
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## Interpretation of Q and $\omega_0$



$$H_{LP}(s) = H_0 \frac{\omega_0^2}{s^2 + \frac{\omega_0}{Q}s + \omega_0^2}$$



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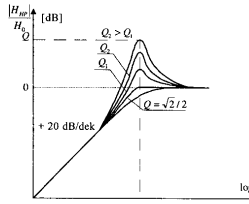
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## Interpretation of Q and $\omega_0$



$$H_{HP}(s) = H_0 \frac{s^2}{s^2 + \frac{\omega_0}{Q}s + \omega_0^2}$$



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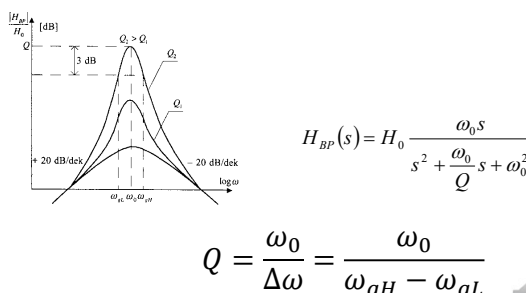
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### Interpretation of Q and $\omega_0$



$$H_{BP}(s) = H_0 \frac{\omega_0 s}{s^2 + \frac{\omega_0}{Q} s + \omega_0^2}$$

$$Q = \frac{\omega_0}{\Delta\omega} = \frac{\omega_0}{\omega_{gH} - \omega_{gL}}$$


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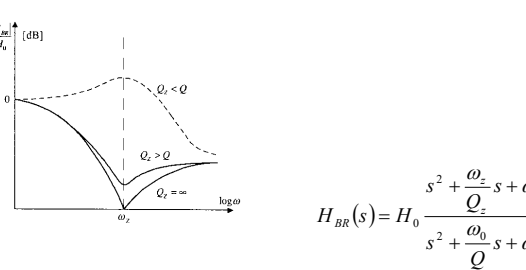
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### Interpretation of Q and $\omega_0$



$$H_{BR}(s) = H_0 \frac{s^2 + \omega_z s + \omega_z^2}{s^2 + \frac{\omega_0}{Q} s + \omega_0^2}$$


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### Filtry aktywne - wprowadzenie

$Q_z = \infty$  - elliptic filter with transfer function:

$$H_{BR}(s) = H_0 \frac{\omega_z^2 \frac{s^2}{\omega_z^2} + 1}{\omega_0^2 \frac{s^2}{\omega_0^2} + \frac{s}{Q\omega_0} + 1}$$


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## Active filters - factorization of LP - prototype filter

Transmittance factorization:

$$H(s) = \frac{A}{D(s)} = \prod_k H_k(s) = \prod_k \frac{A_k}{M_k(s)}$$

order of  $N_k(s) \leq$  order of  $M_k(s) \leq 2$

For order  $M_k(s) = 2$  biquadratic section, or =1 first order section:

$$H_i(s) = \frac{A_i}{a_i s^2 + b_i s + 1} \quad \text{OR} \quad H_j(s) = \frac{A_j}{a_j s + 1}$$


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## Filters transformation

$$S = \frac{s}{\omega_0} \quad H_i(S) = \frac{Ku}{A_i S^2 + B_i S + 1}$$

Low pass filter

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## Bessel Butterworth Chebyshev(I)

N	i	a <sub>i</sub>	b <sub>i</sub>	f <sub>cut/fc</sub>	Q <sub>i</sub>
1	1	1.0000	0.0000	1.0000	-
2	1	1.3614	1.3827	1.0000	0.86
3	1	1.8036	0.0000	0.537	-
3	2	0.6402	1.1911	0.912	1.71
4	1	2.6282	3.4341	0.538	0.71
4	2	0.3648	1.1509	0.919	2.94
5	1	2.9235	0.0000	0.342	-
5	2	1.3025	2.5354	0.881	1.18
5	3	0.2290	1.0833	0.910	4.54
6	1	3.8645	6.9797	0.366	0.68
6	2	0.7528	1.8573	0.878	1.81
6	3	0.1589	1.0711	0.916	6.51
7	1	4.0211	0.0000	0.249	-
7	2	1.8729	4.1795	0.645	1.09
7	3	0.4861	1.5676	0.912	2.58
7	4	0.1156	1.0443	0.910	8.84
8	1	5.1117	11.9607	0.276	0.68
8	2	1.0659	2.9365	0.841	1.61
8	3	0.3439	1.4206	0.914	3.47
8	4	0.0882	1.0407	0.915	11.53
9	1	5.1318	0.0000	0.195	-
9	2	2.4283	6.6307	0.506	1.06
9	3	0.6839	2.2908	0.989	2.21
9	4	0.2359	1.3131	0.914	4.48
9	5	0.0695	1.0272	0.914	14.58
10	1	6.3648	18.3695	0.222	0.67
10	2	1.3582	4.3453	0.689	1.53
10	3	0.4822	1.9440	0.991	2.89
10	4	0.1994	1.2520	0.910	5.61
10	5	0.0563	1.0283	0.910	17.99

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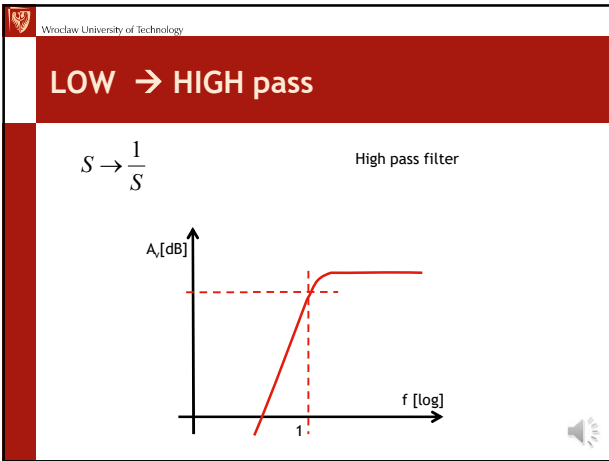
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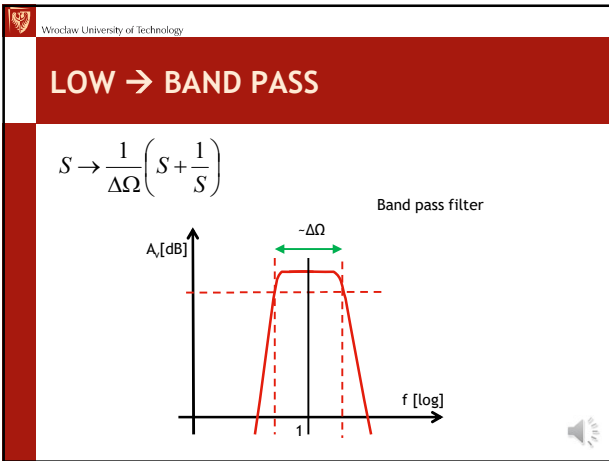
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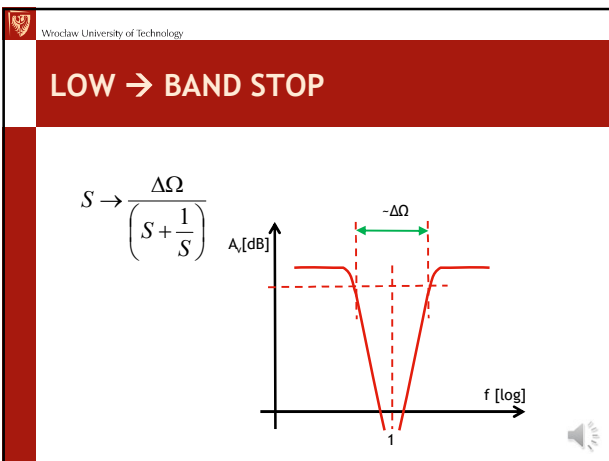
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## Filters transformation

$$S = \frac{s}{\omega_0}$$

$$H_i(S) = \frac{Ku}{A_i S^2 + B_i S + 1}$$

Low pass filter  
And all other kinds of filters

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## Cascade of biquadratic filters

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## LP, BP, HP sections

$\frac{A_i}{a_i s^2 + b_i s + 1}$	$\frac{1}{a_i s + 1}$
$\frac{A_i s}{a_i s^2 + b_i s + 1}$	
$\frac{A_i s^2}{a_i s^2 + b_i s + 1}$	$\frac{s}{a_i s + 1}$

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### 1st order high pass filter

$$A_v = \frac{U_{out}}{U_{in}} = \frac{R}{R + \frac{1}{sC}} = \frac{sCR}{sCR + 1}$$

$$= \frac{R}{R + \frac{1}{j\omega C}} = \frac{1}{1 + \frac{1}{j\omega CR}} = \frac{1}{1 + \frac{1}{j\omega RC}} = \frac{1}{1 + \frac{\omega_0}{j\omega}} = \frac{1}{1 + \frac{f_0}{jf}}$$

$f_0 = \frac{1}{2\pi RC}$

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### 1st order low pass filter

$$A_v = \frac{U_{out}}{U_{in}} = \frac{\frac{1}{sC}}{R + \frac{1}{sC}} = \frac{1}{1 + jsCR}$$

$$= \frac{1}{1 + j\omega \frac{1}{RC}} = \frac{1}{1 + j\frac{\omega}{\omega_0}} = \frac{1}{1 + j\frac{f}{f_0}}$$

$f_0 = \frac{1}{2\pi RC}$

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### Active filters

#### Sallen - Key low pass implementation

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### Sallen - Key low pass implementation

Transmittance:

$$H_{LP}(s) = \frac{U_{wy}(s)}{U_{we}(s)} = \frac{\frac{1+R_4/R_3}{R_1 R_2 C_1 C_2}}{s^2 + \left( \frac{1}{R_1 C_1} + \frac{1}{R_2 C_1} + \frac{R_4/R_3}{R_2 C_2} \right) s + \frac{1}{R_1 R_2 C_1 C_2}}$$

where:

$$\omega_0 = \frac{1}{\sqrt{R_1 R_2 C_1 C_2}} \quad Q = \frac{1}{\left( \frac{1}{R_1 C_1} + \frac{1}{R_2 C_1} + \frac{R_4/R_3}{R_2 C_2} \right)}$$


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### Sallen - Key high pass implementation

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### Sallen - Key high pass implementation

$$H_{HP}(s) = \frac{U_{out}(s)}{U_{in}(s)} = \frac{(1+R_4/R_3)s^2}{s^2 + \left( \frac{1}{R_2 C_1} + \frac{1}{R_2 C_2} + \frac{R_4/R_3}{R_1 C_1} \right) s + \frac{1}{R_1 R_2 C_1 C_2}}$$


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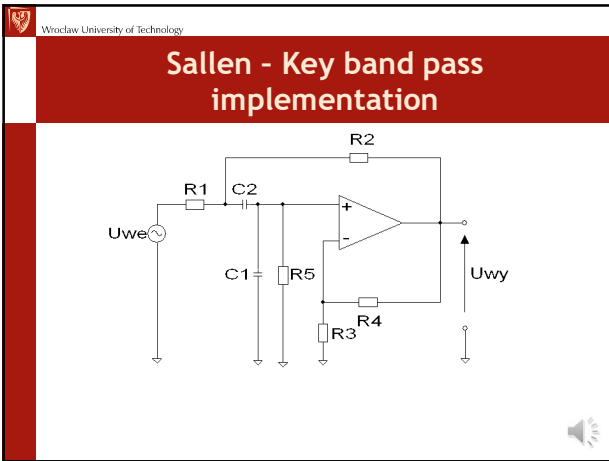
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### Sallen - Key band pass implementation

$$H_{BP}(s) = \frac{U_{out}(s)}{U_{in}(s)} = \frac{\frac{1+R_4/R_5}{R_1 C_1} s}{s^2 + \left( \frac{1}{R_1 C_1} + \frac{1}{R_3 C_2} + \frac{1}{R_5 C_1} + \frac{R_4/R_3}{R_2 C_1} \right) s + \frac{R_1 + R_2}{R_1 R_2 R_3 C_1 C_2}}$$

$$\omega_0 = \sqrt{\frac{R_1 + R_2}{R_1 R_2 R_3 C_1 C_2}} \quad Q = \frac{\sqrt{\frac{R_1 + R_2}{R_1 R_2 R_3 C_1 C_2}}}{\left( \frac{1}{R_1 C_1} + \frac{1}{R_3 C_2} + \frac{1}{R_5 C_1} + \frac{R_4/R_3}{R_2 C_1} \right)}$$

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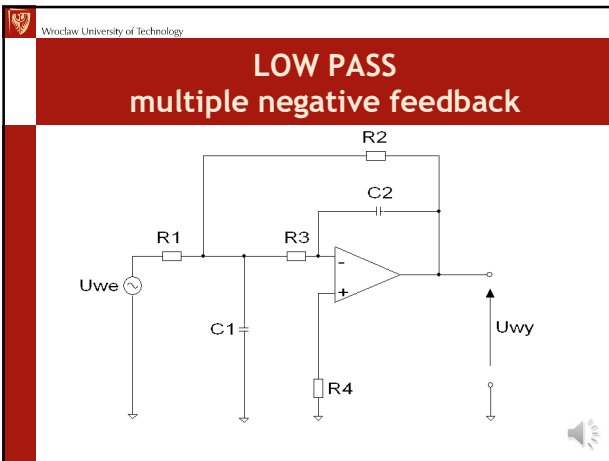
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### LOW PASS multiple negative feedback

$$H_{LP}(s) = \frac{U_{wy}(s)}{U_{we}(s)} = \frac{-\frac{R_2/R_1}{R_2 R_3 C_1 C_2}}{s^2 + \frac{s}{C_1} \left( \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right) + \frac{1}{R_2 R_3 C_1 C_2}}$$

$$\omega_0 = \frac{1}{\sqrt{R_2 R_3 C_1 C_2}} \quad Q = \left[ \sqrt{\frac{C_2}{C_1}} \left( \sqrt{\frac{R_3}{R_2}} + \sqrt{\frac{R_2}{R_3}} + \frac{\sqrt{R_2 R_3}}{R_1} \right) \right]^{-1}$$


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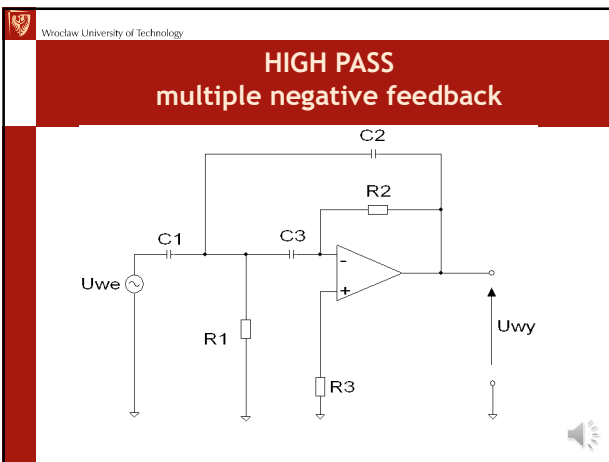
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### HIGH PASS multiple negative feedback

Transfer function:

$$H_{HP}(s) = \frac{U_{out}(s)}{U_{in}(s)} = \frac{-C_1/C_2 s^2}{s^2 + \frac{s}{R_2} \left( \frac{C_1}{C_2 C_3} + \frac{1}{C_2} + \frac{1}{C_3} \right) + \frac{1}{R_1 R_2 C_2 C_3}}$$

where:

$$\omega_0 = \frac{1}{\sqrt{R_1 R_2 C_2 C_3}} \quad Q = \left[ \sqrt{\frac{R_1}{R_2}} \left( \frac{C_1}{\sqrt{C_2 C_3}} + \sqrt{\frac{C_3}{C_2}} + \sqrt{\frac{C_2}{C_3}} \right) \right]^{-1}$$


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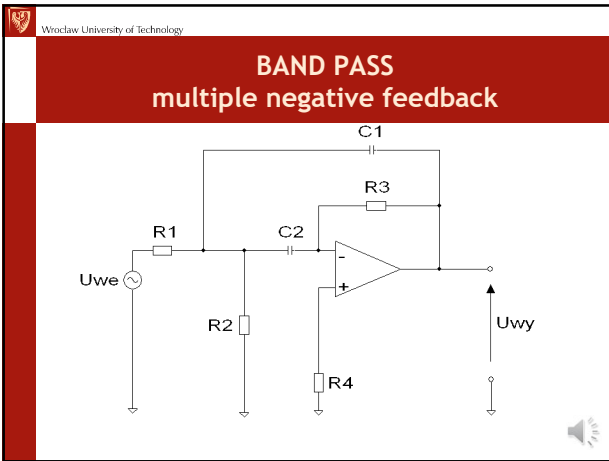
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### BAND PASS multiple negative feedback

$$H_{BP}(s) = \frac{U_{out}(s)}{U_{in}(s)} = \frac{-\frac{s}{R_1 C_1}}{s^2 + s \left( \frac{1}{R_3 C_1} + \frac{1}{R_3 C_2} \right) + \frac{R_1 + R_2}{R_1 R_2 R_3 C_1 C_2}}$$

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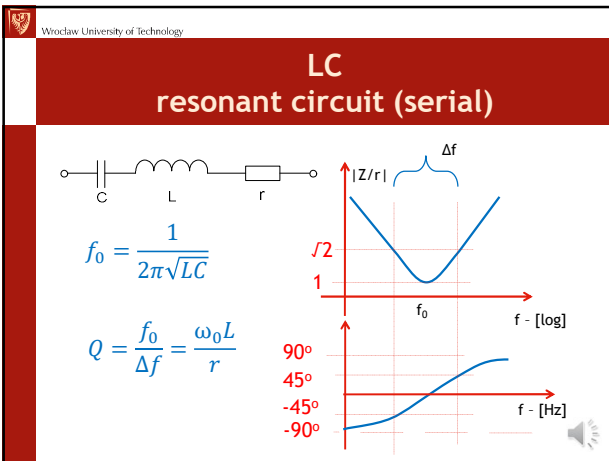
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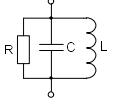
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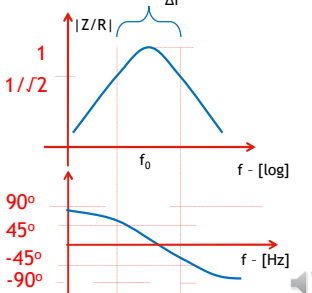
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### LC resonant circuit (parallel)



$$f_0 = \frac{1}{2\pi\sqrt{LC}}$$

$$Q = \frac{f_0}{\Delta f} = \frac{R}{1/\omega_0 C}$$



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### Q-factor definition

$$Q = \frac{f_0}{\Delta f} = \frac{\omega_0}{\omega_{gH} - \omega_{gL}}$$


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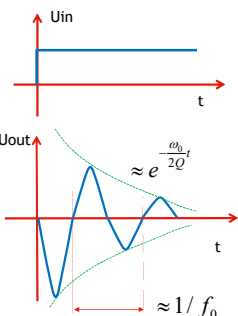
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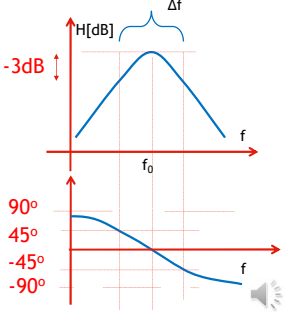
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### Band pass





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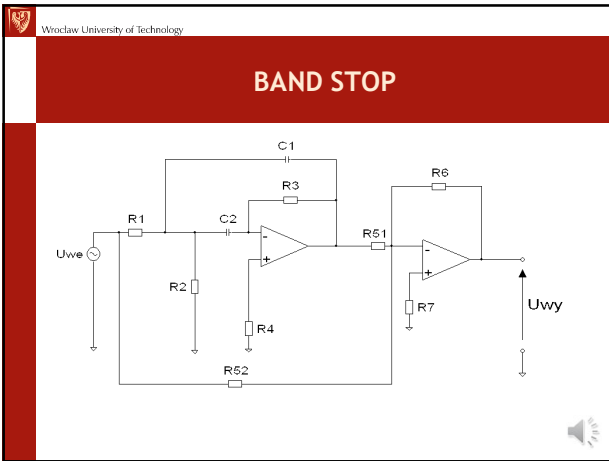
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## Active filters-multiple negative feedback

Transmitancja filtru:

$$H_{BR}(s) = -\left(\frac{R_6}{R_{51}} H_{BP}(s) + \frac{R_6}{R_{52}}\right)$$

Przy częstotliwości środkowej  $\omega = \omega_0$

$$\left. \begin{aligned} |H_{BP}(\omega = \omega_0)| &= 1 \frac{V}{V} \\ \varphi(\omega = \omega_0) &= \pi \end{aligned} \right\} H_{BP} = -1 \frac{V}{V}$$

Dla:  $R_{51} = R_{52} = R$

$$H_{BR}(\omega = \omega_0) = 0$$


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## BAND STOP (NOTCH FILTER)

$f_n = \frac{1}{4\pi RC}$

$C1 = C2 = C$   
 $R4 = R3 = R$   
 $R2 = R1 = R'$   
 $f_0 = \frac{1}{2\pi RC}$

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## ALL PASS FILTER

$$H(s) = \frac{N(s)}{D(s)} = \prod_k H_k(s)$$

$$H_k(s) = \frac{s^2 - b_1s + b_0}{s^2 + b_1s + b_0}$$

$$|H_k(s)| = 1$$



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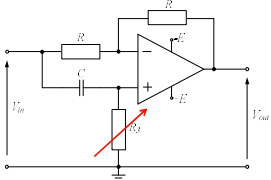
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## phase shifter (all pass filter of 1st order)



$$\frac{V_{out}}{V_{in}} = -\frac{1 - sCR}{1 + sCR}$$



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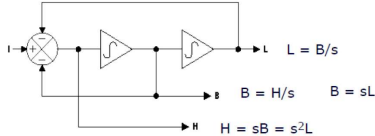
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## state variable filter



$$L = B/s \quad B = sL$$

$$H = sB = s^2L$$

$$H = I - B - L \quad s^2L = I - sL - L$$

$$\frac{L}{I} = \frac{1}{s^2 + s + 1} \quad \frac{B}{I} = \frac{s}{s^2 + s + 1} \quad \frac{H}{I} = \frac{s^2}{s^2 + s + 1}$$



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## Biquadratic monolithic universal filter UF42 by TI (state variable filter)

Note: If  $R_2 = 50k\Omega$ , the external gain-setting resistor can be eliminated by connecting  $V_{in}$  to pin 2.

Pin numbers are for DIP package. SOIC-16 pinout.

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## Switched capacitor filter

$$I = \frac{U}{R}$$

$$I = \frac{dQ}{dt} = \frac{d(UC_s)}{dt} = \frac{UC_s}{T_s} = UC_s f_s$$

$$R = \frac{1}{C_s f_s}$$


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## Switched capacitor circuits

Switched Capacitor Resistor Emulation Circuit	Schematic	Equivalent Resistance
Parallel		$\frac{T}{C}$
Series		$\frac{T}{C}$
Series-Parallel		$\frac{T}{C_1 + C_2}$
Bilinear		$\frac{T}{4C}$

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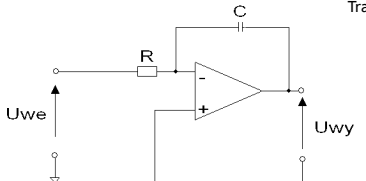
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### C switched filter



Transfer function

$$\frac{U_{wy}}{U_{we}} = -\frac{1}{\tau s}$$

Where:  $\tau = RC$

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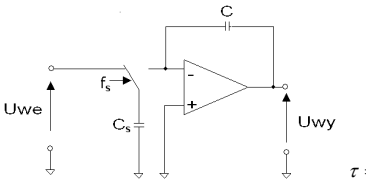
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### C switched filters



Transfer function

$$\frac{U_{wy}}{U_{we}} = -\frac{1}{\tau s}$$

$$\tau = CR_{LAST} = \frac{C}{f_s C_s} = \frac{\eta}{2\pi f_s}$$

$$\frac{\eta}{2\pi} = \frac{C}{C_s}$$

$$\eta = (50 \div 200)$$


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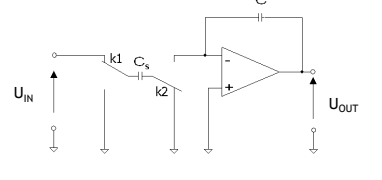
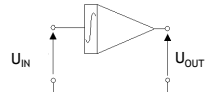
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### C switched integrator


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## C switched integrator

$$\frac{U_{wy}}{U_{we}} = \frac{f_s C_S}{sC} = \frac{1}{s}$$

$$\tau = CR_{ZAST} = \frac{C}{f_s C_S} = \frac{\eta}{2\pi f_s}$$



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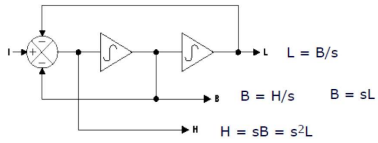
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## state variable filter



$L = B/s$   
 $B = H/s$      $B = sL$   
 $H = sB = s^2L$

$H = I - B - L$      $s^2L = I - sL - L$

$$\frac{L}{I} = \frac{1}{s^2 + s + 1} \quad \frac{B}{I} = \frac{s}{s^2 + s + 1} \quad \frac{H}{I} = \frac{s^2}{s^2 + s + 1}$$



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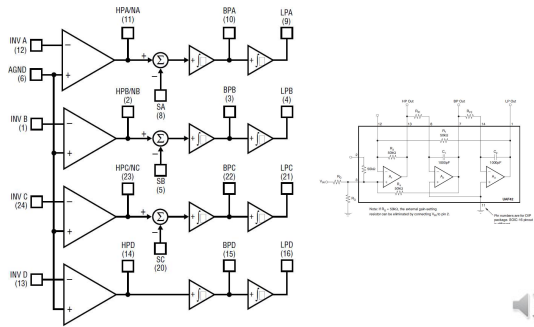

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## 4 biquadratic filters with switched capacitors in LTC1064 by LT


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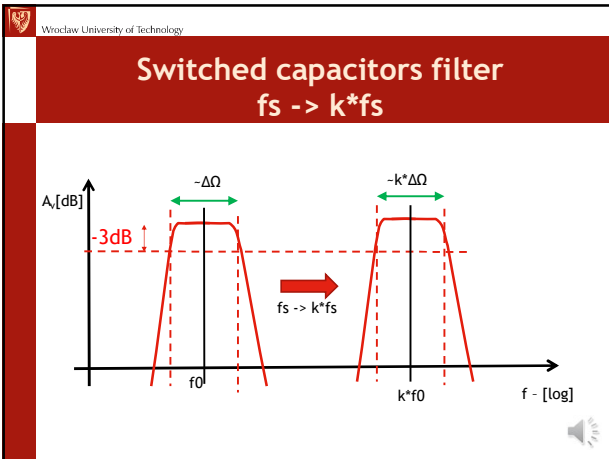
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### Application note of LT(now AD) switched capacitor filters

Worth to be read:

<https://www.analog.com/media/en/technical-documentation/application-notes/an40f.pdf>

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- ### Problems
1. Q-factor of a bandpass filter ?
  2. Types of filters (band stop, b. pass etc.)
  3. Types of frequency response of filters (Bessel, Butterworth, Chebyshev, Elliptic (Cauer)),
  4. Biquadratic filter (biquadratic section)
  5. General idea of C-switching filters

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